

# **Optimal Control Analysis of Cyberattacks in Software-Defined Networking**

By

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# Presentation Outline

- Introduction
- State-of-the-art
- Epidemic Modeling of VIS System
- Solutions and Stabilities Analysis of the Model
- VIS Model Simulation
- Results and Discussions
- Conclusion
- References

# Introduction

- Networking which is basically, the use of computer networks to communicate with other devices digitally happens to be nowadays a crucial part of the live of human being.
- Then, data transmission in a high speed is the most requested by every internet user.

# Introduction

- SDN is a ground-breaking networking model developed to give a new life of visibility and revolution in networking.
- Hence, the success of the SDN is based on the separation of the control plane and data plane, which is responsible for the flexibility, agility and ease manageability of the network.

# Introduction

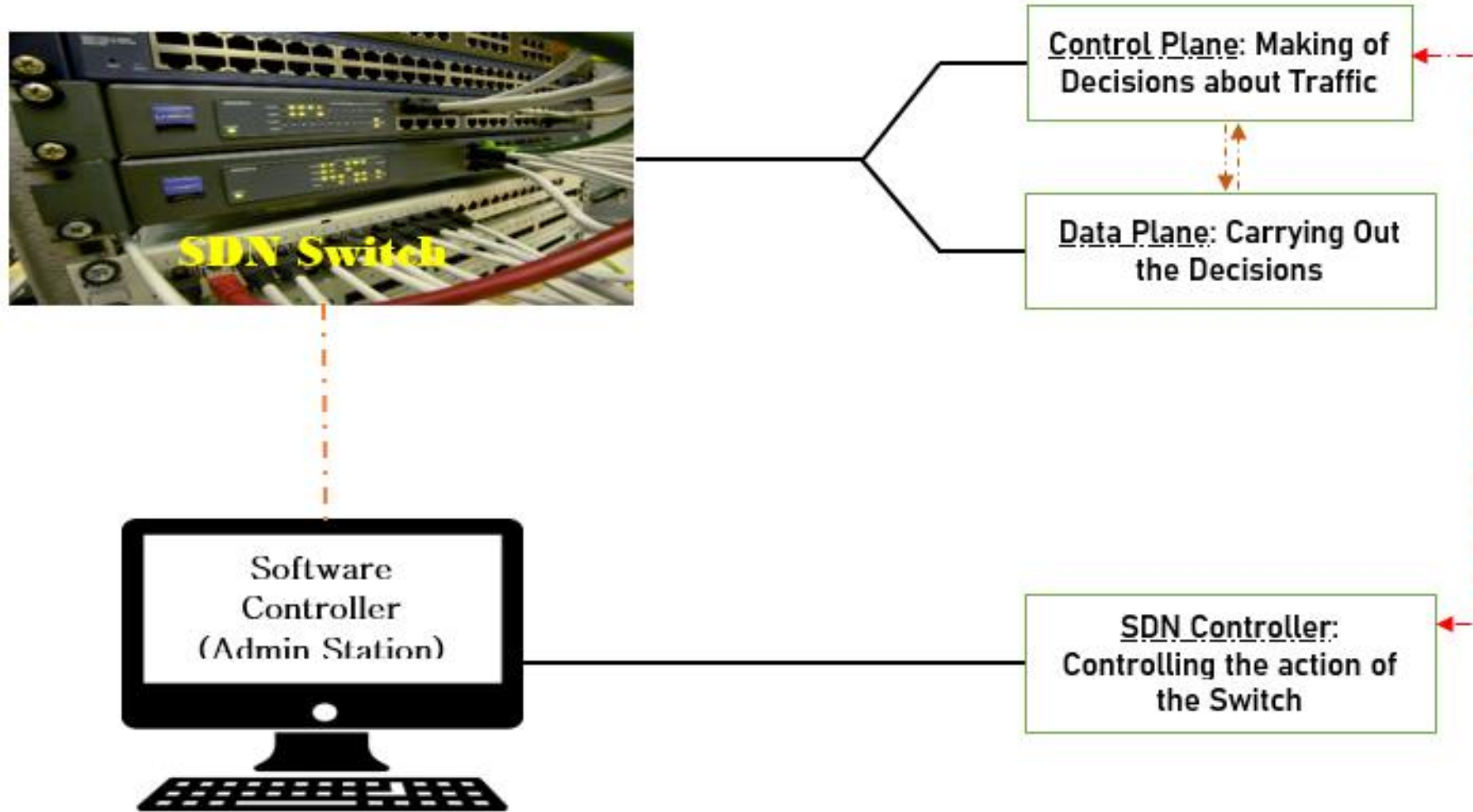


Figure 1: Typical SDN Functioning

# Introduction

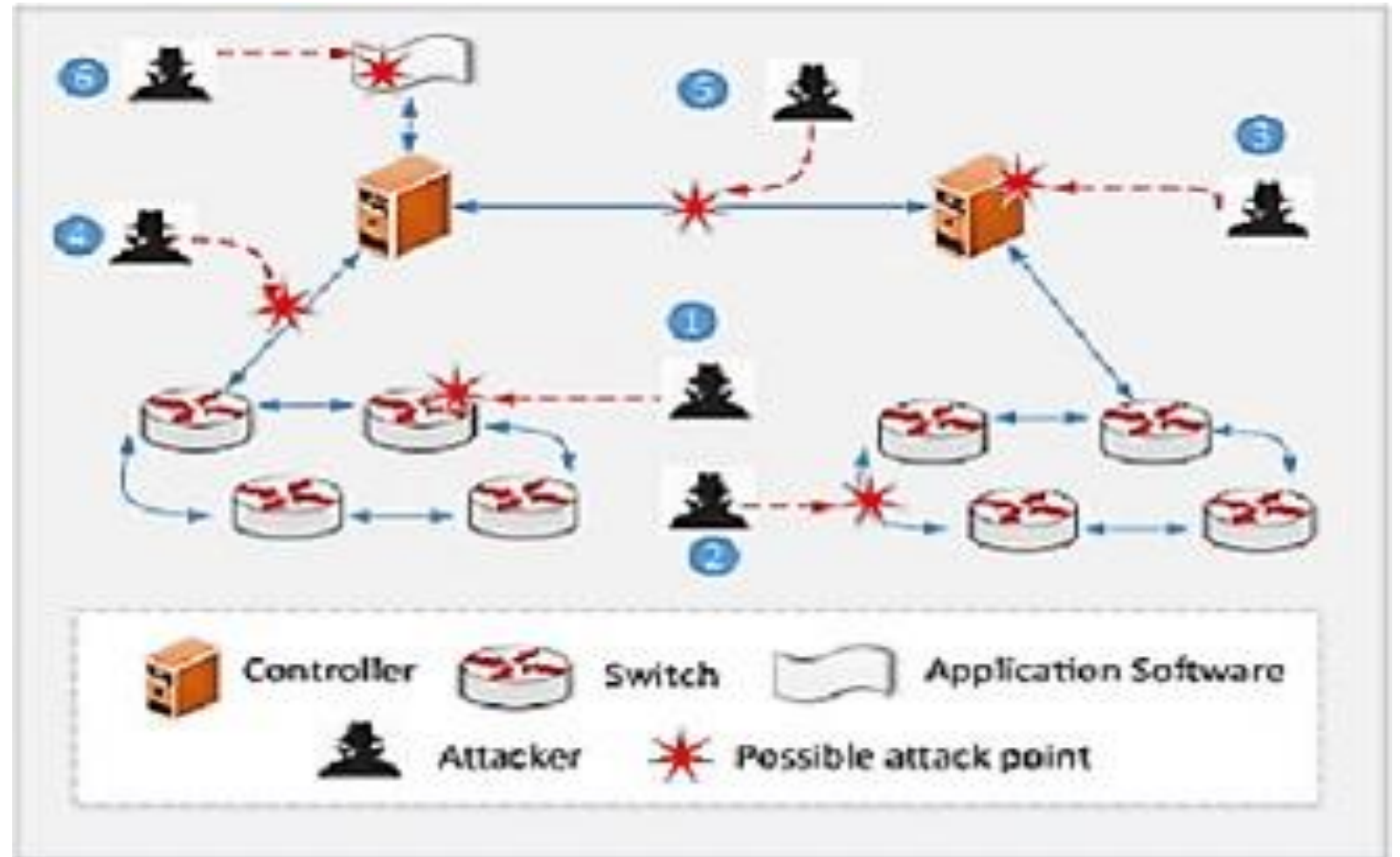
- Many types of cyberattacks such as SQL Injection Attacks, malware, Botnet, DDoS, Probe, User-to-Root attack (U2R), Zero-Day Exploits, Web attack and many more
- are disrupting the emerging technologies such as IoT, SDN, 5G technology, Edge computing, Blockchain, quantum computing, Cloud Computing, Big Data, AI and machine learning.

# Introduction

- The primary goal of any cyberattack is to disrupt the operation of systems, networks, or services (Alasali and Dakkak , 2023).
- The Cyberattackers attempt to bring down the target infrastructure for online services.

# Introduction

- (1) The SDN switch
- (2) The links between SDN switches
- (3) The SDN Controller
- (4) The links between the controller and the switches
- (5) The links between controllers
- (6) The application software



**Figure 2:** Cyberattacks in SDN Paradigm



# State-of-the-art

- Several related works have been consecrated to different types of cyberattacks including epidemic approach ((Wang et al. , 2017), (Nashat et al. , 2021), (Mahboubi et al. , 2017), (Mishra and Saini , 2017), (Yerra et al. , 2017), (Hosseini et al. , 2014), (Androulidakis et al. , 2016) and (Yan and Liu , 2006)).
- That being said, each of these strategies has addressed the impacts of the cyberattacks in networks.

# State-of-the-art

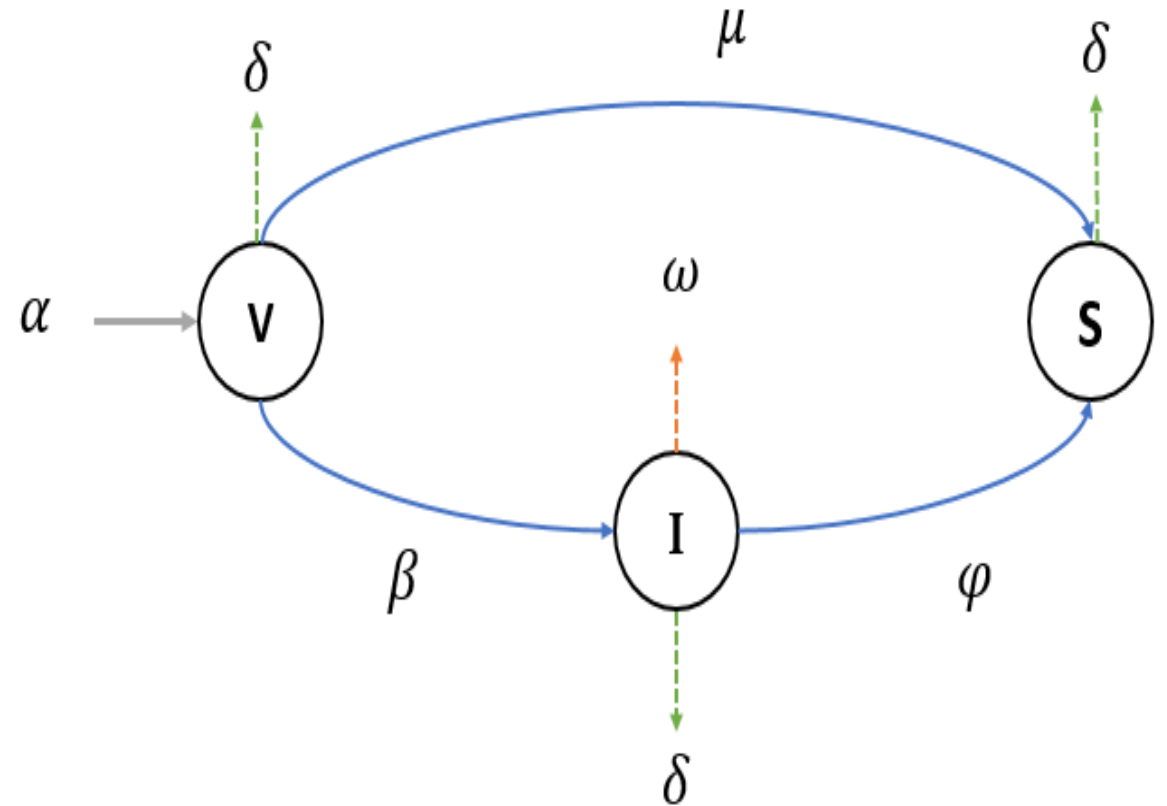
- Some shortcomings in the existing epidemic models have been applied to analyse cyberattacks in SDN.
- The shortcomings include the close-population of nodes, the failure to consider the possibility of a node leaving the network for other reasons unconnected to the attacks and the failure to consider major parameters and assumptions related to network environment.

# State-of-the-art

- The SEIR model in (Androulidakis et al. , 2016) (Yan and Liu , 2006), (Sirijampa et al. , 2018) and (Ajbar and Algahtani , 2020) was proposed to demonstrate how quickly the malware spread over the networks.
- Yet, the authors assumed a close-population of nodes, that is, new nodes joining the network during the instance of analysis is not permitted.

# Epidemic Modeling of VIS System

- Hence, the infection of nodes behaves in a similar way as human epidemic such as the novel COVID-19.
- (V) Vulnerable class of nodes.
- (I) Infected class of nodes.
- (S) Secured class of nodes



**Figure 3:** Representation of the Proposed VIS Model.

# Solutions and Stabilities Analysis of the Model

- Matching ODE for the proposed VIS epidemic model.
 
$$\begin{cases} \frac{dV}{dt} = \alpha - \beta VI - \mu V - \delta V \\ \frac{dI}{dt} = \beta VI - \varphi I - \delta I - \omega I \\ \frac{dS}{dt} = \varphi I + \mu V - \delta S \end{cases} \quad (1)$$

$$(V, I, S) \in \mathbb{R}^3, \begin{cases} V > 0 \\ I \geq 0 \\ S \geq 0 \end{cases}$$

- Equilibria point of VIS model.
- Every equation in the system (1) will be equal to zero.

$$\begin{cases} \alpha - \beta VI - \mu V - \delta V = 0 \\ \beta VI - \varphi I - \delta I - \omega I = 0 \\ \varphi I + \mu V - \delta S = 0 \end{cases} \quad (2)$$

# Solutions and Stabilities Analysis of the Model

- Attack-free Equilibrium.
- At a point where there is no attack in the integration of SDN and 5G, that particular stage is epidemically called attack-free equilibrium point.
- By solving the system (3), the VIS model will be free from attack at  $(V^0, I^0, S^0)$ .

$$\begin{cases} \alpha - \beta V^0 I^0 - \mu V^0 - \delta V^0 = 0 \\ \beta V^0 I^0 - \varphi I^0 - \delta I^0 - \omega I^0 = 0 \\ \varphi I^0 + \mu V^0 - \delta S^0 = 0 \end{cases} \quad (3)$$

$$\begin{cases} V^0 = \frac{\alpha}{\mu + \delta} \\ I^0 = 0 \\ S^0 = \frac{\mu \alpha}{\delta(\mu + \delta)} \end{cases} \quad (4)$$

# Solutions and Stabilities Analysis of the Model

- Local Stability of DDoS-free Equilibrium.

$$\begin{cases} \frac{dV}{dt} = \alpha - \beta VI - \mu V - \delta V = 0 \\ \frac{dI}{dt} = \beta VI - \varphi I - \delta I - \omega I = 0 \\ \frac{dS}{dt} = \varphi I + \mu V - \delta S = 0 \end{cases} \quad (5)$$

- “J” is set as the Jacobian Matrix of the system (5) equation.

$$J^* = \begin{pmatrix} -\beta I^0 - \mu - \delta & -\beta V^0 & 0 \\ \beta I^0 & \beta V^0 - \varphi - \delta - \omega & 0 \\ \mu & \varphi & -\delta \end{pmatrix} \quad (6)$$

- The system (7) is gotten by considering the equation (4).

$$J^* = \begin{pmatrix} -\mu - \delta & -\frac{\beta\alpha}{\mu+\delta} & 0 \\ 0 & \frac{\beta\alpha}{\mu+\delta} - \varphi - \delta - \omega & 0 \\ \mu & \varphi & -\delta \end{pmatrix} \quad (7)$$

- With the  $(3 \times 3)$  Jacobian matrix, three eigenvalues are obtained after solving the determinant of  $|J^* - I\psi| = 0$ .

$$\begin{cases} \psi_1 = -\delta \\ \psi_2 = -\mu - \delta \\ \psi_3 = \frac{\beta\alpha - (\mu + \delta)(\varphi + \delta + \omega)}{\mu + \delta} \end{cases} \quad (8)$$

# Solutions and Stabilities Analysis of the Model

- BRN is found from  $\psi_3$ , the eigenvalue that is not obviously negative out of the three.

$$\frac{\beta\alpha - (\mu + \delta)(\varphi + \delta + \omega)}{\mu + \delta} < 0 \quad (9)$$

$$\frac{\beta\alpha}{(\mu + \delta)(\varphi + \delta + \omega)} < 1 \quad (10)$$

$$R_0(V, I, S) = \frac{\beta\alpha}{(\mu + \delta)(\varphi + \delta + \omega)}, (\mu + \delta)(\varphi + \delta + \omega) \neq 0 \quad (11)$$

- The attack decreases and will probably dies out when  $R_0 < 1$ .
- The attack is stable without any new infectious node in the system when  $R_0 = 1$ .
- The attack increases in the system when  $R_0 > 1$ .



# Solutions and Stabilities Analysis of the Model

- The Hopf bifurcation around the endemic point E2 is satisfied by the  $\delta^* = \frac{\beta + \alpha}{I^* + S^*}$
- The adequate condition for the system to have a hopf bifurcation at E2 given by  $T(\delta^*) = 0$
- The Jacobian matrix is obtained by solving the determinant of  $|J^0 - I\psi| = 0$ .

$$\begin{cases} -(\delta I_2 + \alpha) - \psi_V = 0 \\ \delta V_2 - (\beta + \alpha) - \psi_I = 0 \\ -\alpha - \psi_S = 0 \end{cases} \quad (20)$$

# Solutions and Stabilities Analysis of the Model

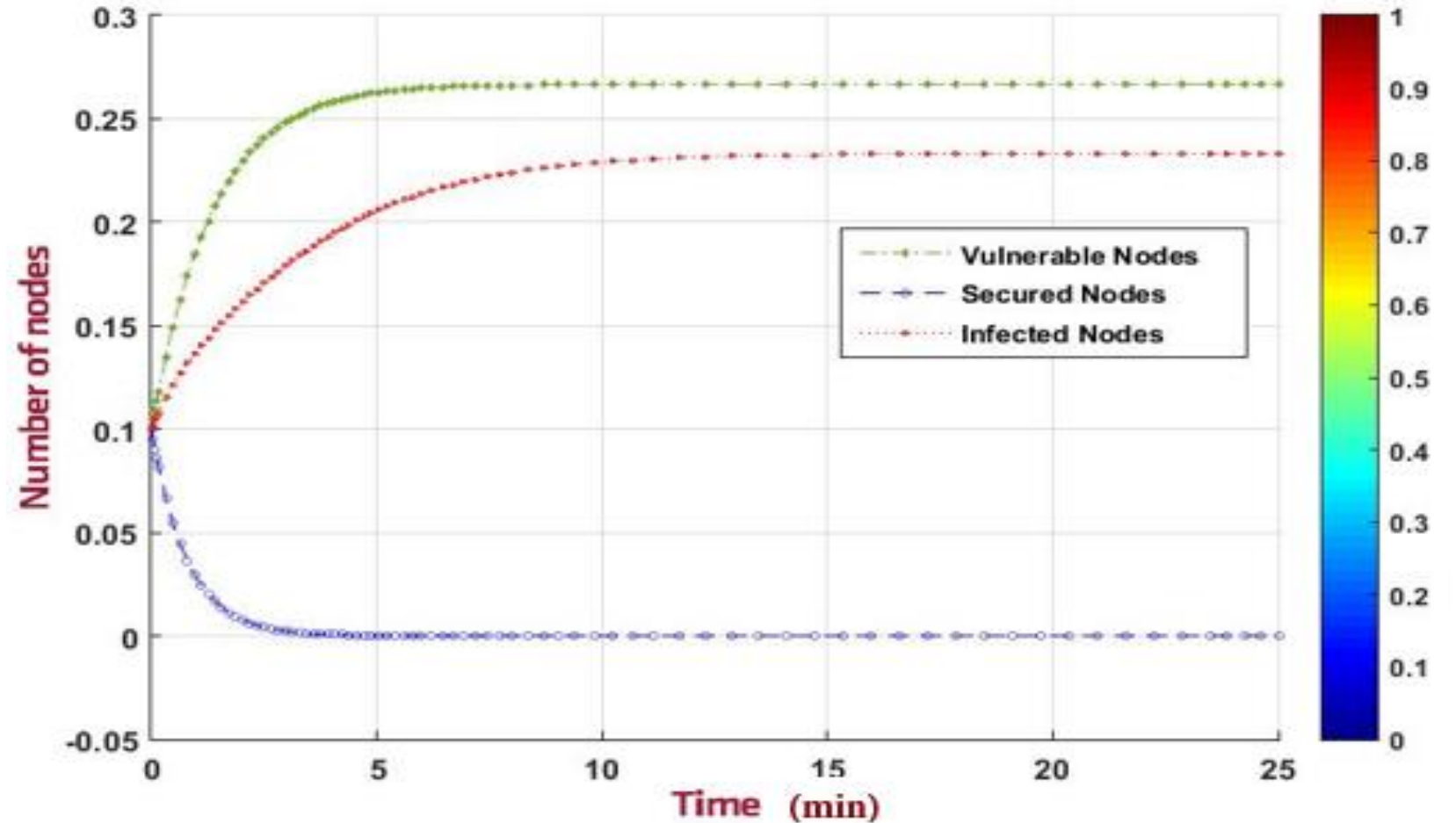
- The eigenvalues is presented in equation (21) below

$$\begin{cases} \psi_V = -(\delta I_2 + \alpha) \\ \psi_I = \delta V_2 - (\beta + \alpha) \\ \psi_S = -\alpha \end{cases} \quad (21)$$

- Therefore, for  $\alpha > 0$  the eigenvalue  $\psi_S$  is negative while the root of the remaining two eigenvalues are complex conjugate.
- Consequently, the condition for the Hopf bifurcation is satisfied at  $\delta = \delta^*$ .
- Since,  $\frac{dT}{d\delta} = S_2 \neq 0$ .

# Results and Discussions

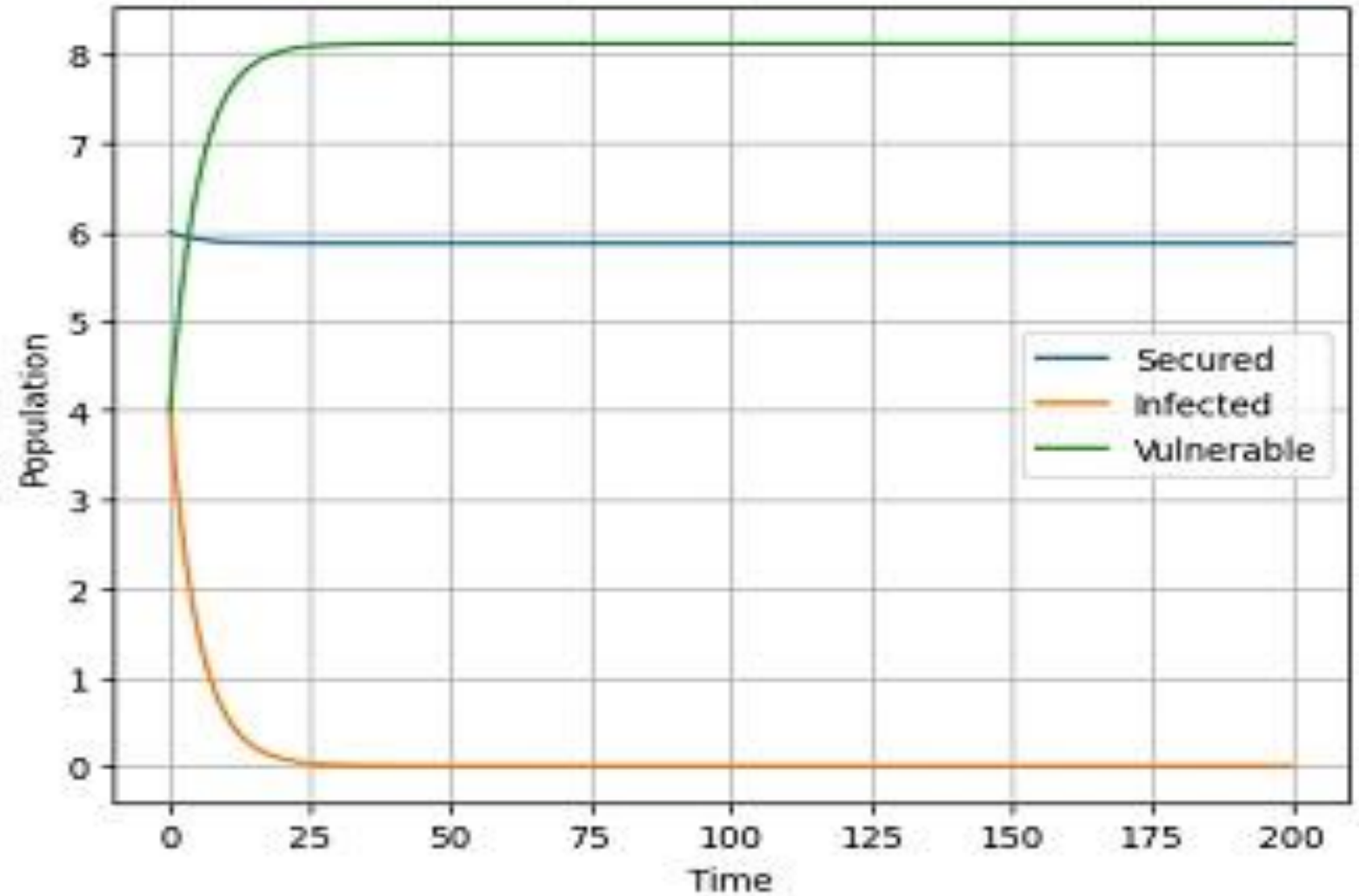
- Figure 3 presents the graphical representation of the three classes of nodes (V, I, S).



**Figure 4:** General Stability of the VIS Model.

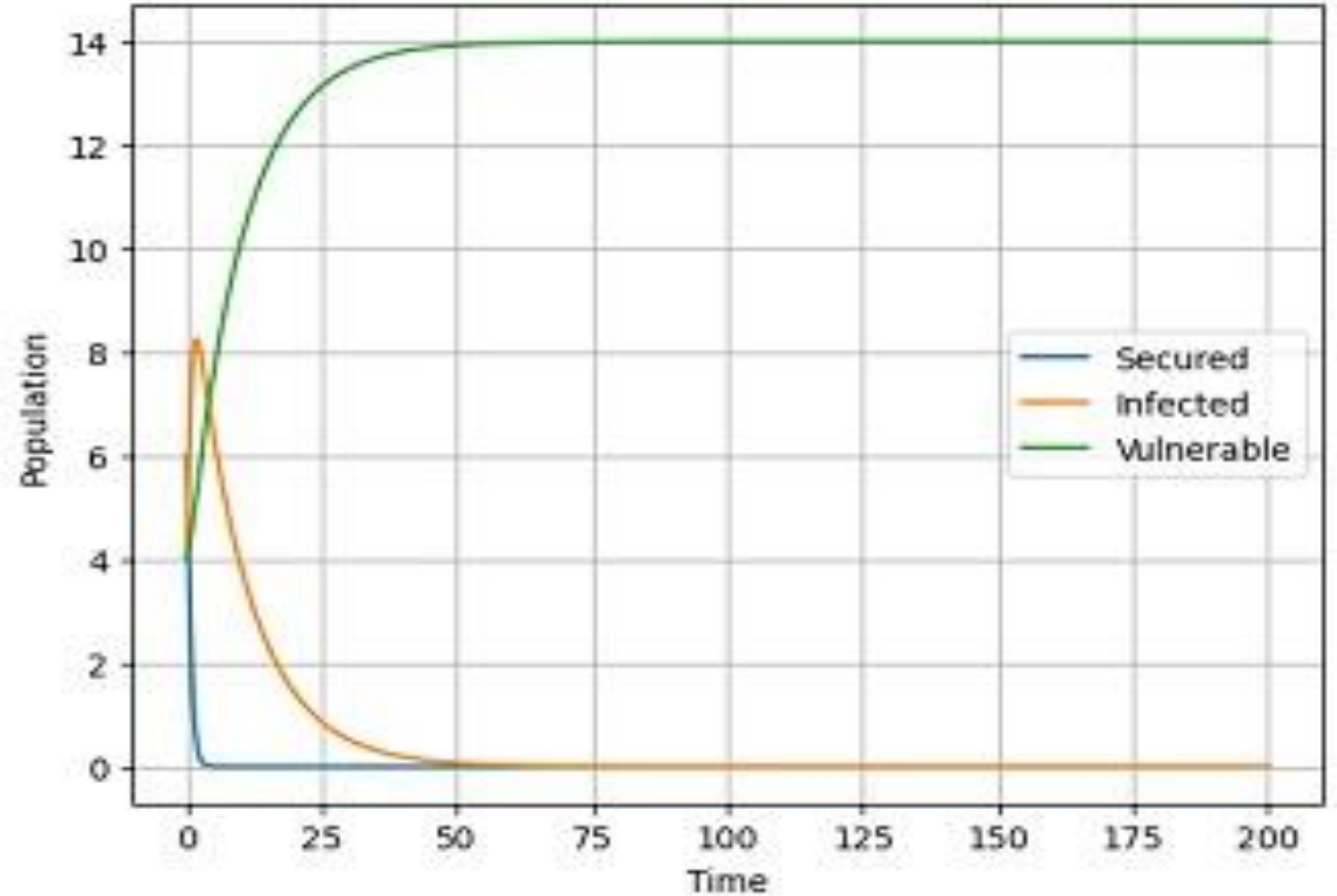
# Results and Discussions

- Figure 5:  
Bifurcation  
Occurs at the  
Attacks-Free  
Equilibrium  
Point With  $\beta$   
 $= 0.03$

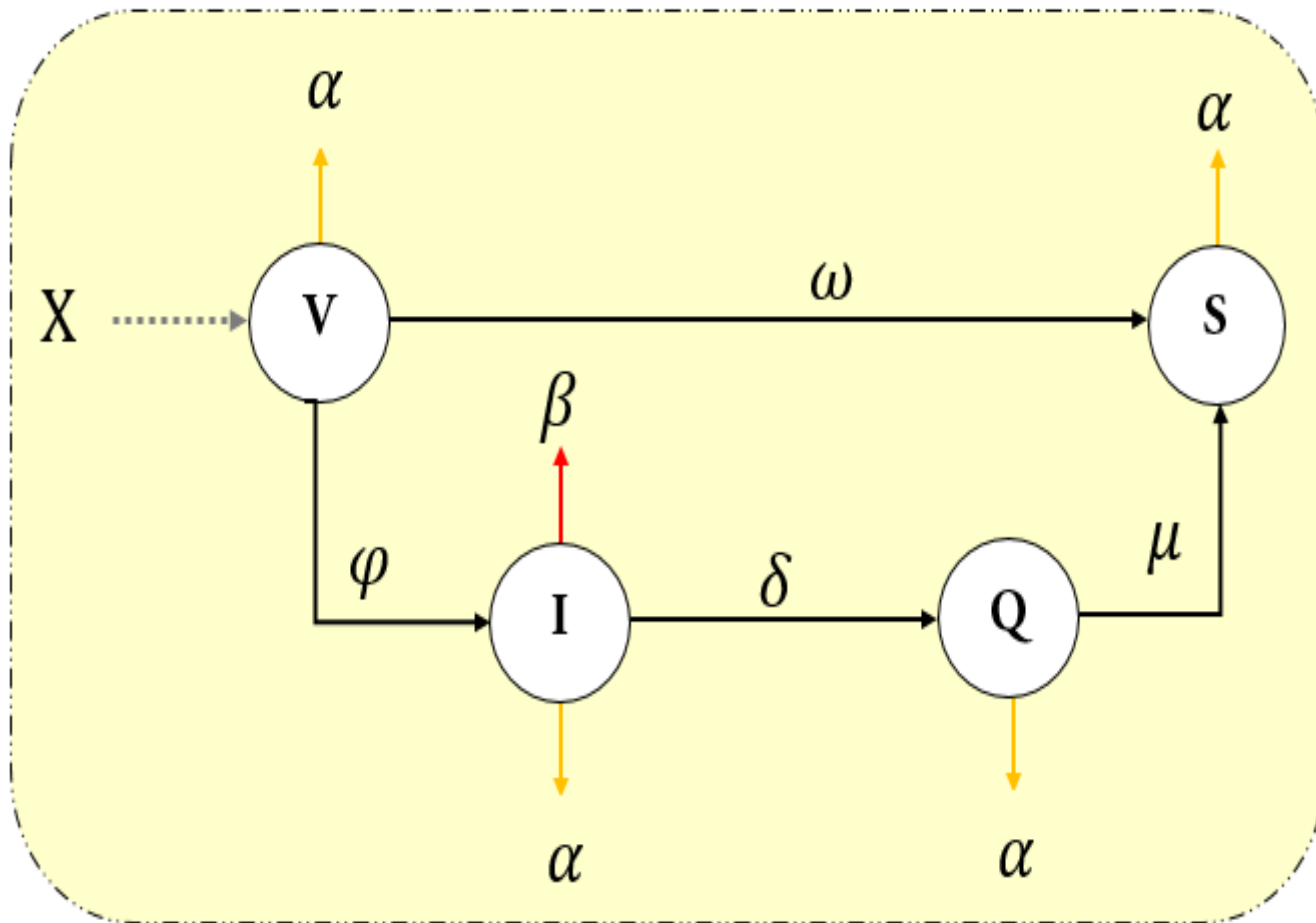


# Results and Discussions

- Figure 6:  
Bifurcation  
Occurs at the  
Attacks-Free  
Equilibrium  
Point With  $\beta =$   
0.2



# Optimal Control Analysis



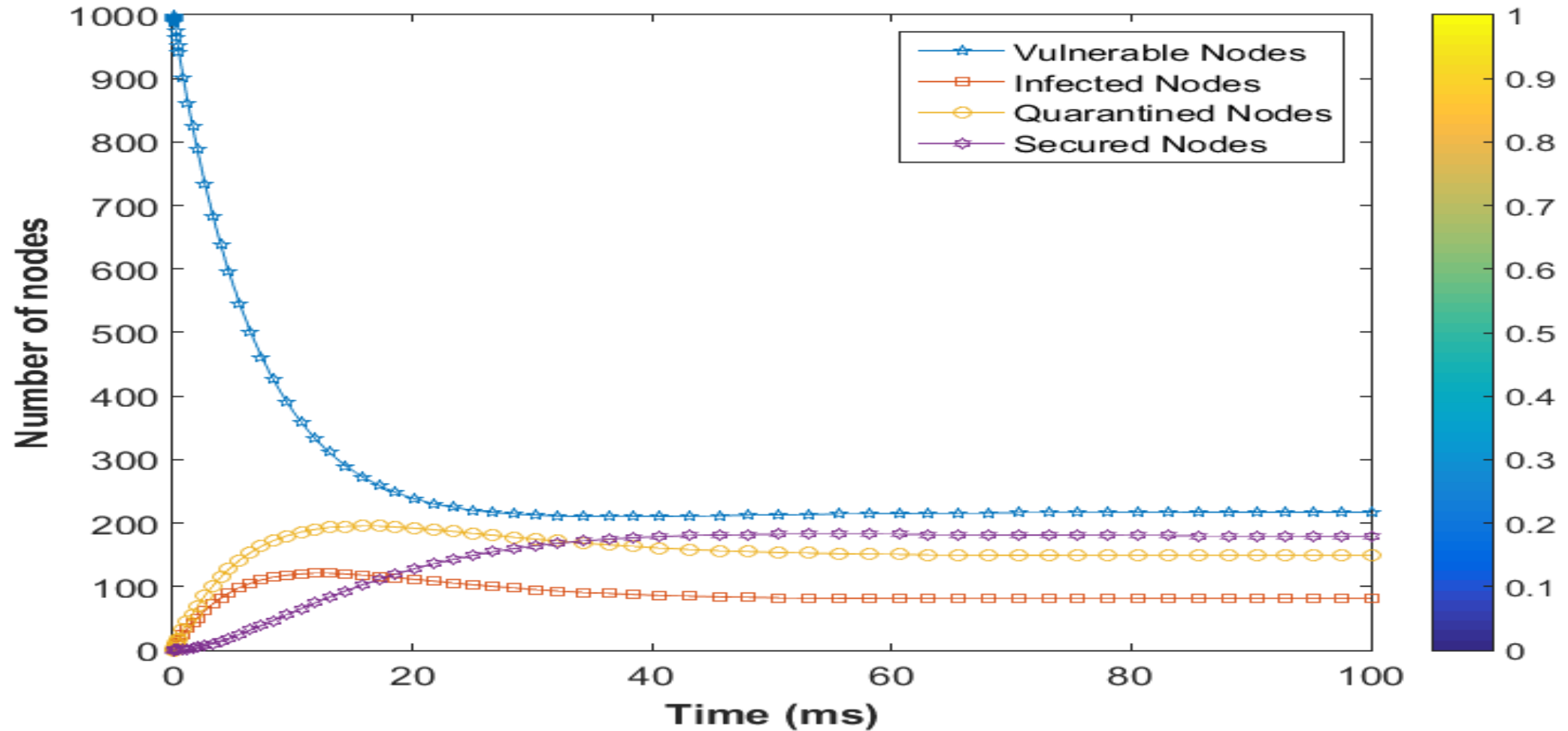
$$X - \varphi VI - \omega V - \alpha V = 0$$

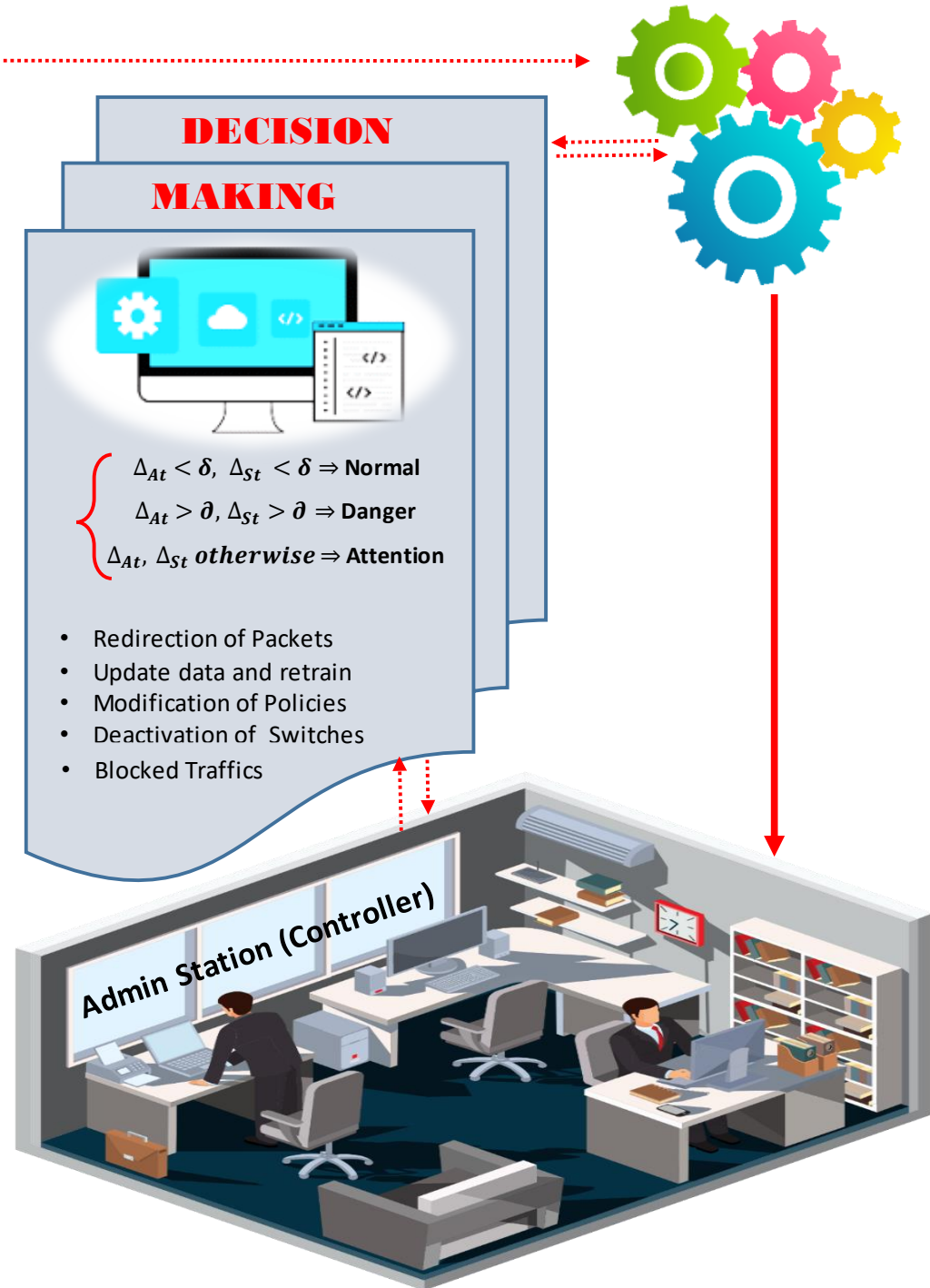
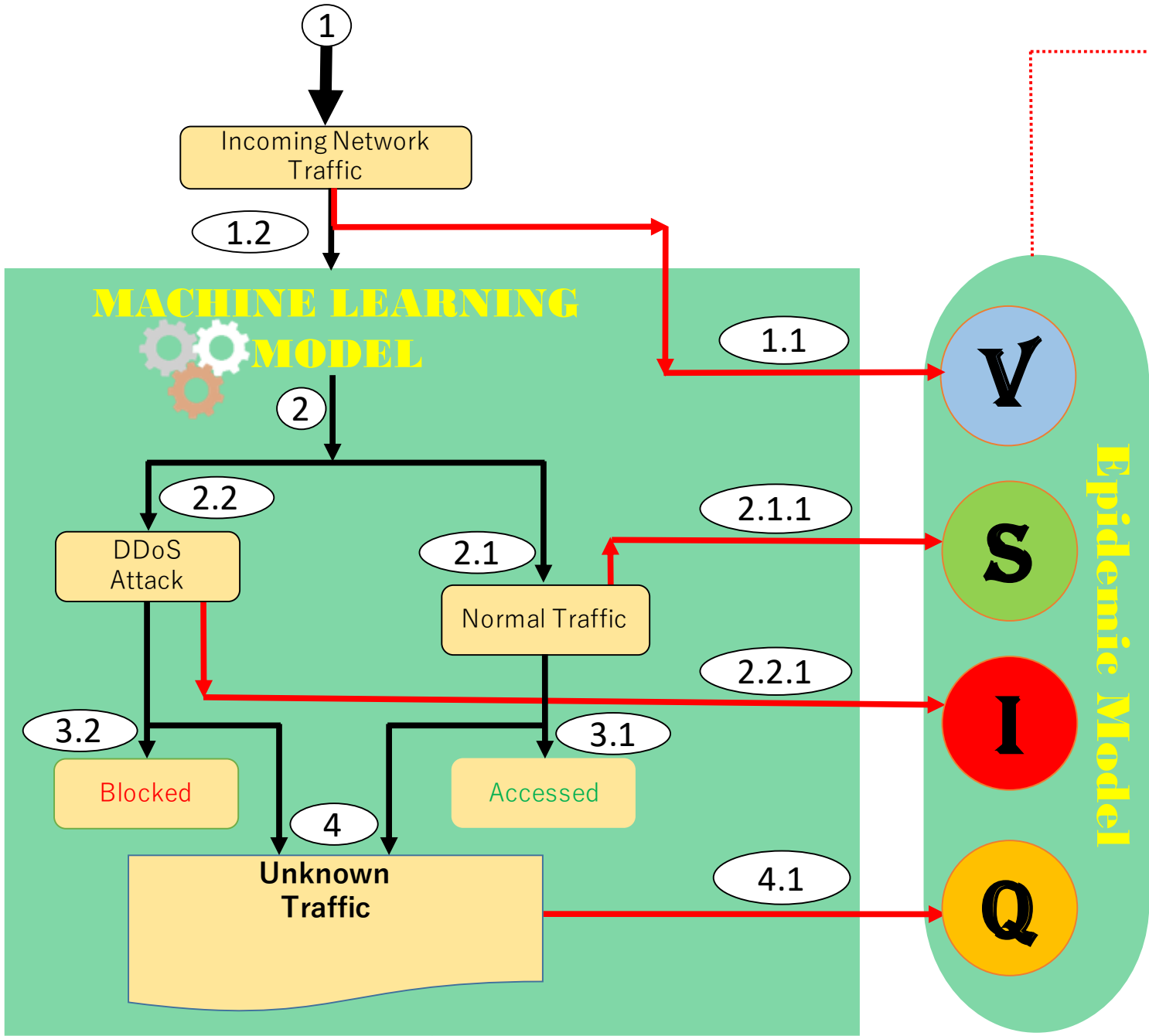
$$\varphi VI - \delta I - \alpha I - \beta I = 0$$

$$\delta I - \mu Q - \alpha Q = 0$$

$$\mu Q + \omega V - \alpha S = 0$$

# Optimal Control Analysis







# Conclusion

- To evaluate the impact of control measures, the model is reformulated as an optimal control problem incorporating the quarantined class of nodes and mitigation strategies.

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**Thanks for listening**